



Use of 3D gravity inversion to aid seismic migration-velocity building

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Abstract

We develop a new tool for initial seismic migration-velocity model building based on a recent gravity inversion method. This method consists of an iterative algorithm that provides a 3D density-contrast distribution on a grid of prisms, the starting point being a user-specified prismatic element called “seed”. By means of this technique of planting anomalous densities, we are able to interpret multiple bodies with different density contrasts. Therefore, the method does not require the solution of a large equation system, which greatly reduces the computational demand. Once the geometry of the anomalous-density body is known, we can extract the skeleton of the inverted body and fill each prism with a velocity consistent with the presumed geology. Starting at this velocity model, the next step is to perform a migration velocity analysis (MVA). The result of MVA can then, in turn, be used to improve on the geometry for the gravity inversion. This joint processing and interpretation can be considered as an alternative way to improve the knowledge of complex structures. For example, the image quality of salt structures and sub-salt sediments obtained by reflection seismic is almost always limited by the effects of wavefield transmission, scattering and absorption. Simple synthetic examples show the capacity of the proposed velocity-model-building algorithm to generate initial velocity models for depth-migration velocity analysis, including those for specific geological targets.

Introduction

Time and depth migration are two fundamental processes in seismic imaging that are regularly applied to seismic data. For their success, high-quality velocity models are indispensable. However, automatic and/or efficient velocity-model construction tools are still a challenge. Most present-day model-building techniques are iterative procedures that improve a starting model based on intermediate results.

Examples for new algorithms for time-migration velocity analysis based on prestack time migration (PSTM), which bypass the conventional CMP-based velocity analysis, are presented in Fomel (2003), Schleicher et al. (2008),

Schleicher and Costa (2009), Coimbra et al. (2013a,b, 2014) and Santos et al. (2014a).

While time migration is more robust and tolerant to velocity errors, methods acting in the depth-domain are more precise. Prestack depth migration (PSDM) techniques are capable of imaging more complex structures including lateral velocity variation and dipping reflectors (Liu and Bleistein, 1995; Liu, 1997). This is so because depth migration is highly sensitive to the velocity model (Zhu et al., 1998). Its strong dependence on a precise velocity model makes PSDM an interesting tool for velocity analysis (Abbad et al., 2009; Mulder and ten Kroode, 2002; Al-Yahya, 1989). On the other hand, a more accurate velocity model is required for its application, which almost always increases the computational cost. This, in turn, leads many researchers to search for alternative methods.

In an attempt to aid the search for more efficient model-building tools, we develop a new 3D algorithm for initial-velocity-model building based on geometry information obtained by means of an efficient gravity-inversion method (Uieda and Barbosa, 2012a,b). First tests on data from simple synthetic models show that this method's consistent estimation of the geometry of bodies with density anomalies can be successfully employed for initial migration-velocity-model building. Further tests on more realistic data are required to evaluate the method's potential for practical applications.

Methodology

In the gravity-inversion method of Uieda and Barbosa (2012a,b) the solution “grows” iteratively around user-specified “seeds” (Figure 1a). Seeds are specified medium cells where the inversion parameters, here the density contrast, is set to a nonzero value. In each iteration, a seed grows by the accretion of one of its neighbouring prisms (Figure 1b). Two criteria must be fulfilled for a neighbouring prism to be chosen for accretion: it must (i) decrease the total data-misfit function and (ii) produce the smallest value of the objective function compared with all other prisms that fulfill the first criterion. A seed grows when at least one of its neighbouring prisms satisfies these criteria. The growth process ends when no seed is able to grow in a given iteration (Figure 1c). During the growth process, the density contrast in the seed and all subsequently accreted prisms is held constant at its initially chosen value. In this way, the method will find the best possible geometry of a density-anomaly body to fit the data with the given perturbation value.

There are at least two advantages in the application of this method: the implementation of a “lazy evaluation” of the sensitivity matrix and the use of the “shape-of-anomaly” data-misfit function of René (1986) together

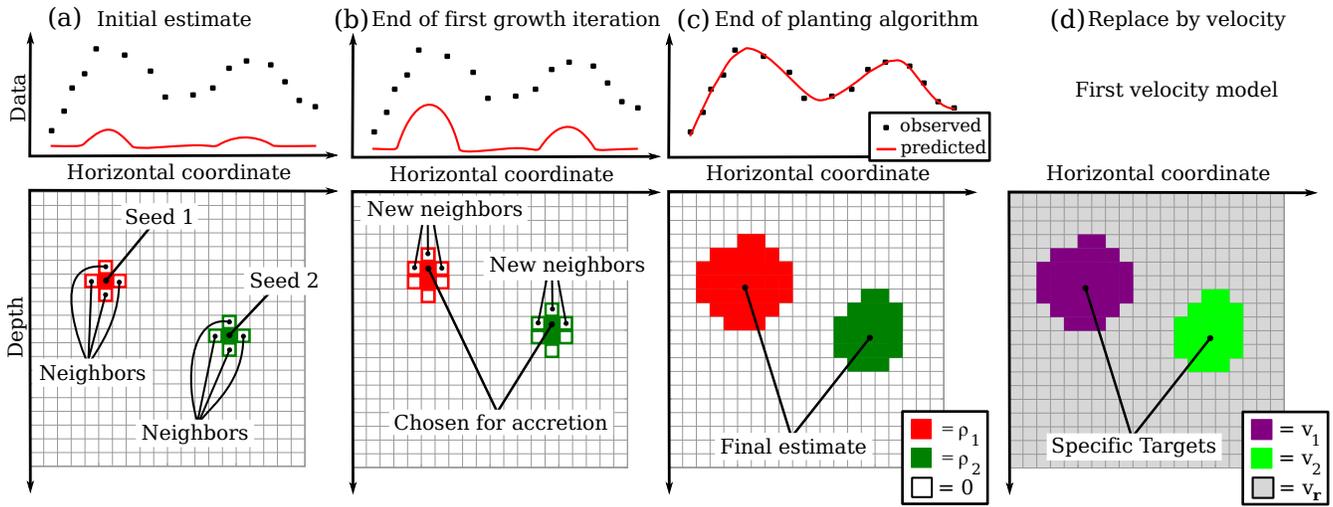


Figure 1: (a-c) Two-dimensional sketch of the three stages of the planting algorithm (extracted from Uieda and Barbosa, 2012a). Black dots represent the observed data and the red line represents the predicted data produced by the current estimate. The light gray grid of prisms represents the interpretative model. (a) Initial state including user-specified seeds with a nonzero density perturbation. (b) End of the first growth iteration where two accretions took place, one for each seed. (c) Final estimate at the end of the algorithm. (d) Two-dimensional sketch of the initial velocity model obtained by replacement of densities by velocities.

with the traditional ℓ_2 -norm data-misfit function (Uieda and Barbosa, 2012b). This implies that the algorithm allows for a fast and memory-efficient inversion, requiring only a small number of seeds, because it considers only the differences in anomaly shape between the observed and predicted data and is insensitive to differences in amplitude.

Here, we use the shape of the estimated density-contrast distribution (i.e., the geometric skeleton of the body) as a first guess for the geometry of a corresponding inclusion in the velocity model and replace the density value contained in each prism by a velocity consistent with the presumed geology (Figure 1d). The associated initial velocity values might be available from borehole data or from previous seismic measurements.

The next step consists of evaluating the quality of this velocity model through the application of migration-velocity-analysis (MVA) techniques. Their results and interpretation, in turn, can not only help to improve the velocity values, but can also allow to extract information that helps to improve on the geometry for the next gravity inversion, thus forming a joint method.

Application to Pluto model

We tested if the geometry of complex structures such as salt structures obtained by gravity inversion is sufficiently well approximated to build a seismic velocity model. As in Santos et al. (2013, 2014b), we performed an inversion of some 3D bodies with different geometries. To demonstrate the capability of the technique, we extracted 2D profiles from the inverted solution, and replaced the density value by a consistent and convenient velocity. Thereafter, we performed 2D depth-migration for seismic data previously modeled with the real geometry using the velocity model of each extracted profile.

For the forward modeling of the gravity data and the

gravity inversion, we used the formulas of Nagy et al. (2000). Together with the inversion method of planting anomalous density seeds (Uieda and Barbosa, 2012a,b), these formulas are implemented in the toolkit *Fatiando a Terra* (Portuguese for “Slicing the Earth”) of Uieda et al. (2014), a freely available open-source Python package for modeling and inversion in geophysics. To perform the necessary seismic processing, we used the open-source software package *Madagascar* (Fomel et al., 2013).

We used the right part of the 2D Pluto model (see Figure 2). The Pluto dataset is one of several test sets released by the Subsalt Multiples Attenuation and Reduction Technology Joint Venture (SMAART JV). It is designed to emulate deep water subsalt prospects as found in the Gulf of Mexico.

From this model we created a 3D salt body to be used in the gravimetric modeling (see the dark red body in Figure 3(a)). To create this 3D body from the 2D model, we proceeded as follows: (i) We extracted the 2D salt body by masking the 2D Pluto model with the proper velocity (4500 m/s). This is the central slice of the yet-to-be 3D salt body. (ii) We then extrapolated the 2D slice laterally in the y -direction by concatenating to both sides a set of modified slices. Each slice to be concatenated was smoothed with increasing window and then masked again with the same velocity value as before.

For the gravimetric modeling, we discretized the so-constructed 3D salt body using 120,960 small prisms with density contrast -0.3 g/cm^3 (Figure 3(a)). The modeled g_z -component is depicted by the color-scale map in Figure 3(b). It was calculated on a regular grid of 151×115 observation points in the x - and y -directions, totaling 17,365 observations, with a grid spacing of 53.34 m in both directions. We then contaminated these modeled data with pseudorandom Gaussian noise with zero mean and 0.1 mGal standard deviation. As for the first example,

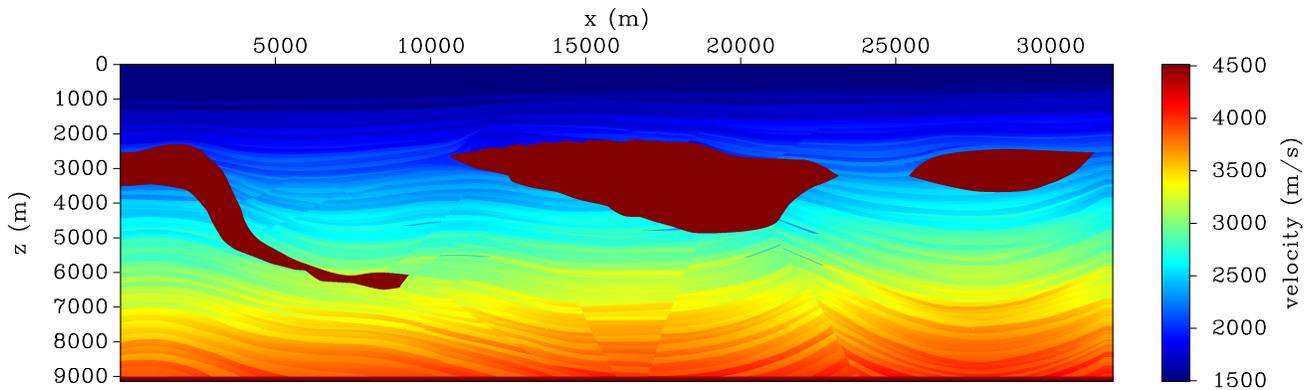


Figure 2: Pluto stratigraphic velocity model. We used the right-most part beyond $x = 23000$ m down to a depth of 8000 m.

we used only a single seed at the center of the simulated body (i.e., at $x = 4500$ m, $y = 3000$ m, and $z = 3000$ m, see Figure 3(a)) to start the gravimetric inversion, which was performed considering an interpretative model consisting of a regular grid of 128,000 prisms, with $\mu = 0.1$ and $\delta = 0.0001$. The black contour lines in Figure 3(b) show the predicted data of the g_z -component produced by the estimated density-contrast distribution (blue prisms in Figure 3(c)). We see that the predicted density distribution fits with the original source structure in all directions.

For the seismic evaluation, we again performed extended split-step Fourier migrations. We used the available Pluto model shot records, sampled at 8 ms. Out of the available 694 shots, we used 51. Their positions are indicated as red stars in all velocity models in this section. The shots were located at 7.62 m depth and are spaced at 137.16 m. We used 150 equally spaced frequencies from 8.0 Hz to 40.4 Hz in the migration process.

For a detailed analysis of the velocity-building process, we migrated the data with five velocity models: (i) constant (water) velocity equal 1500 m/s (Figure 4); (ii) constant vertical-gradient velocity obtained by the function $v(z) = (1500 + 0.235z)$ m/s (Figure 5); (iii) smoothed background with no salt body created using the true stratigraphy velocity (Figure 6); (iv) velocity model obtained by replacement of the density value contained in each prism by a velocity consistent with the presumed geology superimposed onto the above background model (Figure 7). Here we set the velocity inside the predicted body to 4500 m/s surrounded by smoothed values of the true model; (v) true stratigraphic velocity of the Pluto model (Figure 8).

The migrated images presented in these figures prove that imaging the bottom of salt structures is not a simple task, even if we have a sediment model close enough to the real scenario, such as the smoothed background velocity model in Figure 6(a). On the other hand, all these “wrong” results demonstrate the possibility to estimate the top of salt by means of very simple velocity models. Although it is true that they carry errors in the vertical position, any of these initial estimates can be used as a first guess to guide the planting of the seeds or to reduce the number of cells in the mesh of the gravity inversion. Once the salt body has been estimated and inserted into the background model, further migration-velocity analysis can be used to improve

the so-obtained initial model.

Our final result in Figure 7 confirms the quality of the proposed technique. We see that even for this rough estimate of the salt geometry, the resulting velocity model (Figure 7(a)) used for depth-migration (Figure 7(b)) resulted in a satisfactory migrated image of the salt bottom (compare with the image from the true model in Figure 8(b)). We emphasize that for the salt-geometry estimation, we made use of the simplest possible version of the gravity inversion procedure. It used only one iteration with a single seed, without any previous information or preprocessing.

If this simplistic procedure fails, it can be improved in different aspects. It is possible to add more information for the first inversion of gravimetric data, in the form of a more instructed distribution of seeds. To the same end, we can iterate the gravimetric inversion, until the resulting velocity model is acceptable for seismic migration. In each iteration, we can make use of the geometry information from previous iterations to improve our guess for the spacial position of the seeds. Of course, geometric information from intermediate migrations can also be used to improve the seed positioning.

Conclusion

We have studied 3D velocity model building making use of information from gravity inversion. The particular inversion method used is based on planting seeds of anomalous densities and letting the resulting bodies grow. This inversion method has been proven to be efficient in estimating a 3D density-contrast distribution on a grid of prisms. For this purpose, it does not require the solution of a large equation system, which greatly reduces the computational demand.

For its use in seismic migration, we extracted the geometrical skeleton of the inverted body and filled each prism with a velocity consistent with the presumed geology. Because of the very fast construction of the anomalous body, this procedure is an attractive way to improve the knowledge of complex structures, for example, salt structures and sub-salt sediments, in regions of large velocity contrasts, where the seismic imaging is limited by the effects of wavefield transmission, scattering and absorption. Tests on several synthetic data demonstrated the capability of our method to construct initial velocity

models that are useful for depth migration of the seismic data, even though they will generally need subsequent improvement by means of a migration-velocity analysis.

Based on the experiments reported here, we propose the following processing sequence. The top-of-salt is to be estimated from first seismic images with simple velocity models. From this information, we then determine where to introduce targeted seeds for the gravity inversion, which in turn will provide the first estimate for the bottom-of-salt interface. In this way, it should be possible to eliminate the need for the salt-flooding step in the conventional processing sequence, needed to image the bottom-of-salt. In more regular geologic environments, it might even be possible to build a macrovelocity model before the seismic data are acquired, that is, from the gravity (or gravity gradient) inversion alone, if acceptable velocity values can be inferred from the gravity data by means of relations like the Gardner formula (Gardner et al., 1974). This will be useful to help plan the seismic survey and for Quality Control (QC) during acquisition.

Future research will have to show whether the proposed procedure can be used to extract the shape of the salt body with sufficient precision for improved subsalt-velocity-model building with less iterations than conventionally necessary. For this purpose, we need to test the joint method on more realistic data to evaluate the computational cost in the presence of more complex and realistic geology like deep marine salt bodies, with hydrocarbon reservoirs, salt feeders, channels, faults, internal sutures and heterogeneous salt cap and many others important structures that are challenges for geophysical prospection.

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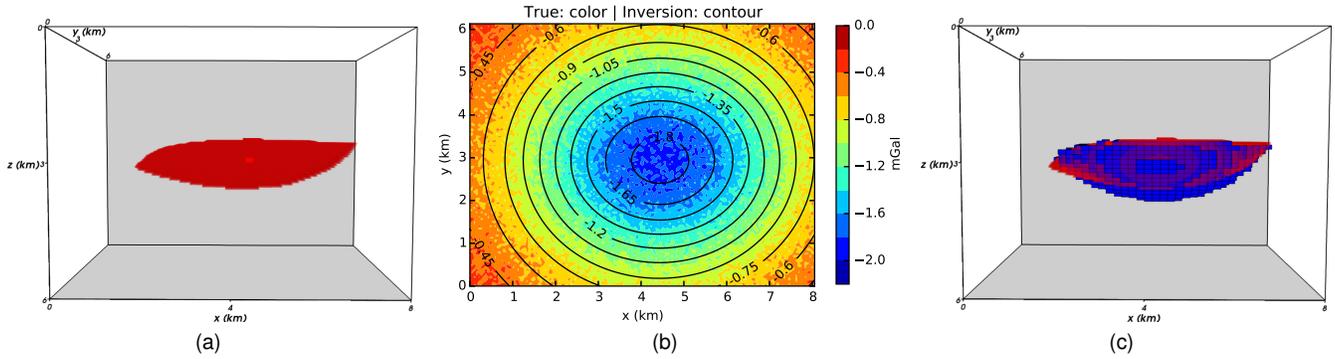


Figure 3: Application to the Pluto salt model. (a) View of the synthetic salt structure used to generate the gravity data (dark red), and the seed used to start the inversion (light red). (b) Synthetic data with noise (color-scale map) and its corresponding predicted data by the inversion result (black contour lines). (c) Estimated geometry of the inverted body (blue) together with original source geometry (red).

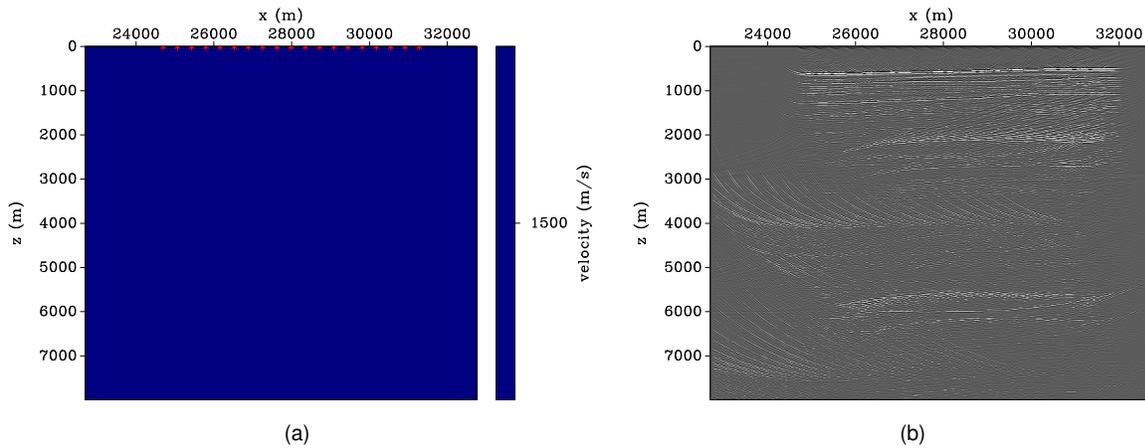


Figure 4: Pluto model test. (a) Constant velocity model with water velocity 1500 m/s. (b) Corresponding migrated image.

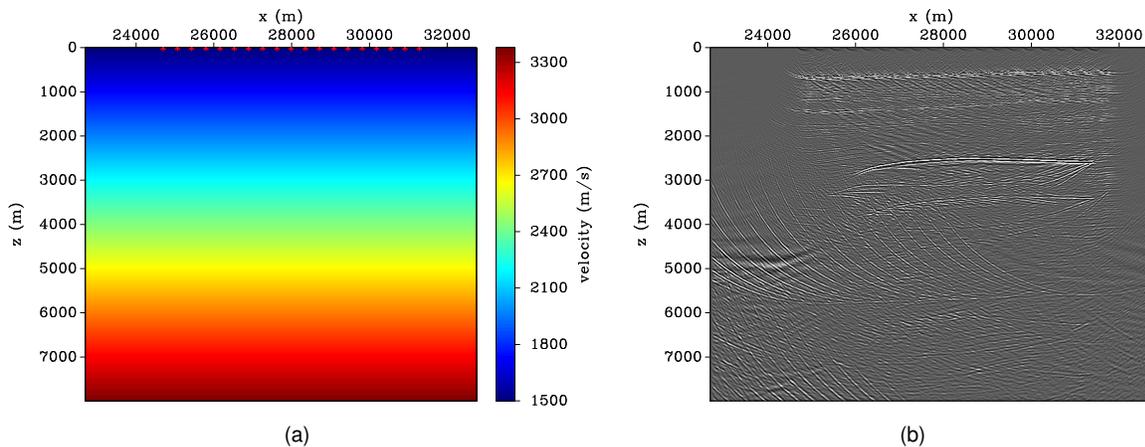


Figure 5: Pluto model test. (a) Constant-gradient velocity model. (b) Corresponding migrated image.

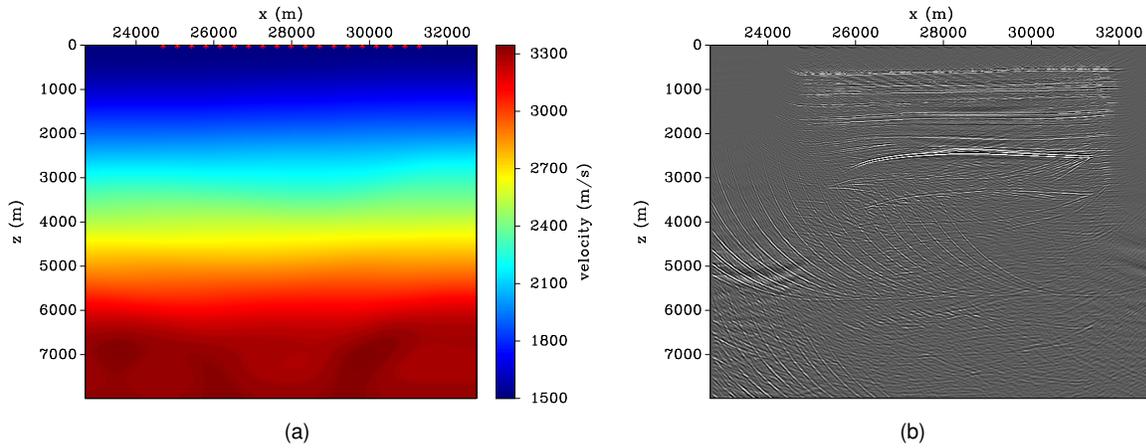


Figure 6: Pluto model test. (a) Background model obtained from smoothing the rightmost part of the true stratigraphy velocity depicted in Figure 2. (b) Corresponding migrated image.

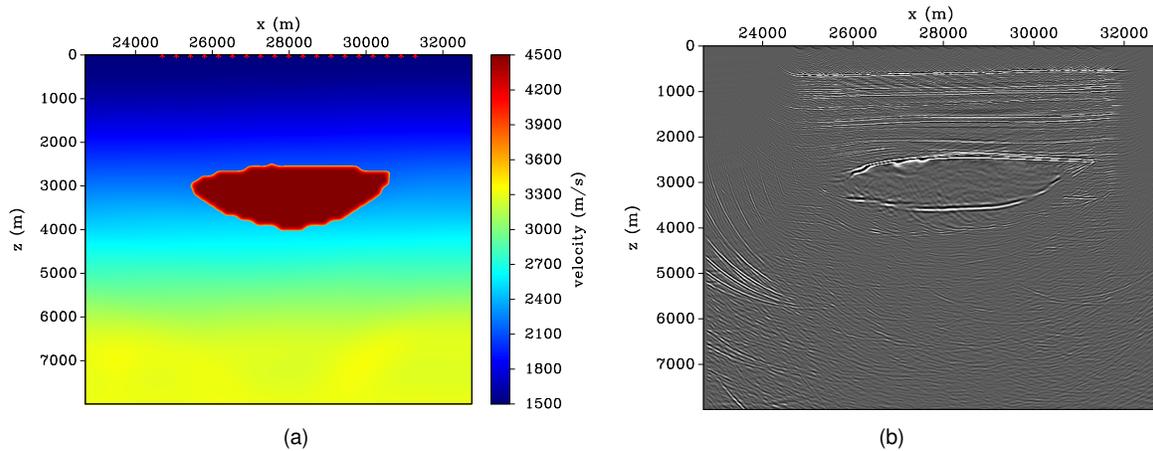


Figure 7: Pluto model test. (a) Model obtained from insertion of a salt body with the geometry from gravity inversion into the background model of Figure 6(a). (b) Corresponding migrated image.

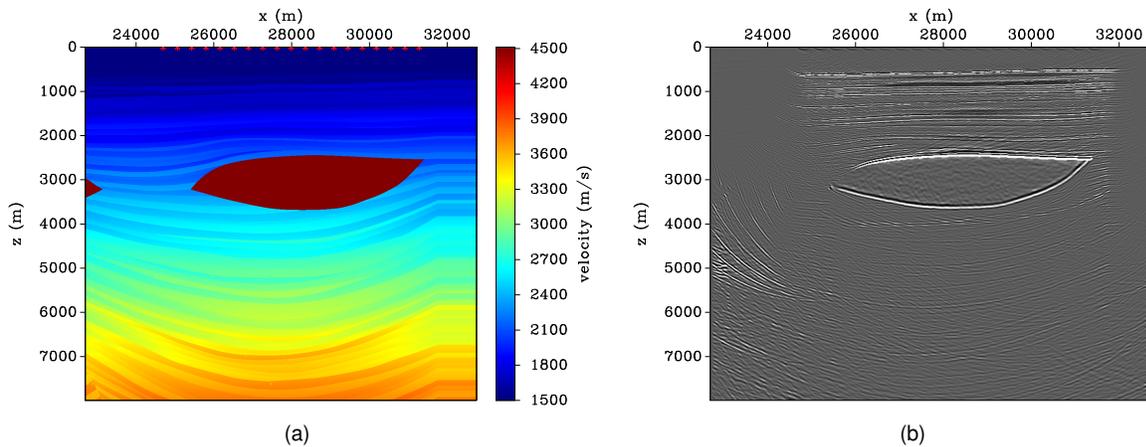


Figure 8: Pluto model test. (a) True stratigraphic model. (b) Corresponding migrated image.